

$$1. 21 + \sqrt{2x-7} = x$$

$$\sqrt{2x-7} = x - 21 \quad |^2$$

$$2x - 7 = x^2 - 42x + 441$$

$$0 = x^2 - 44x + 448$$

$$0 = (x - 28)(x - 16)$$

$$x_1 = 28$$

$$x_2 = 16$$

(28)

$$\text{Let: } x = 16$$

$$L = 21 + \sqrt{32-7} = 21 + 5 =$$

$$P = 16 = 26 \quad L \neq P$$

$$x = 28$$

$$L = 21 + \sqrt{49} = 21 + 7 = 28$$

$$P = 28$$

$$2. 3 + \sqrt{x-1} = x$$

$$\sqrt{x-1} = x - 3$$

$$x - 1 = x^2 - 6x + 9$$

$$0 = x^2 - 7x + 10$$

$$0 = (x - 5)(x - 2)$$

$$x_1 = 5$$

$$x_2 = 2$$

(5)

$$\text{Let: } x = 5$$

$$L = 3 + \sqrt{5-1} = 3 + 2 = 5$$

$$P = 5 \quad L = P$$

$$x = 2$$

$$L = 3 + \sqrt{2-1} = 3 + 1 = 4$$

$$P = 2 \quad L \neq P$$

$$3. \sqrt{2(x-3)} = 3-x \quad |^2 \quad (3)$$

$$2(x-3) = 9-6x+x^2$$

$$2x-6 = 9-6x+x^2$$

$$x^2-8x+15=0$$

$$(x-3)(x-5)=0$$

$$\frac{x_1=3}{x_2=5}$$

$$\text{Kli: } x=3$$

$$L = \sqrt{2(3-3)} = 0$$

$$P = 3-3 = 0$$

$$L=P$$

$$x=5$$

$$L = \sqrt{2(5-3)} = 2$$

$$P = 3-5 = -2$$

$$L \neq P$$

$$4. \sqrt{5-x^2} = x-1 \quad |^2 \quad (2)$$

$$5-x^2 = x^2-2x+1$$

$$0 = 2x^2-2x-4$$

$$0 = x^2-x-2$$

$$0 = (x-2)(x+1)$$

$$\frac{x_1=2}{x_2=-1}$$

$$\text{Kli: } x=2$$

$$L = \sqrt{5-4} = 1$$

$$P = 2-1 = 1$$

$$L=P$$

$$x=-1$$

$$L = \sqrt{5-1} = 2$$

$$P = -1-1 = -2$$

$$L \neq P$$

$$5. \sqrt{x^2+8} = 2x+1 \quad |^2 \quad (1)$$

$$x^2+8 = 4x^2+4x+1$$

$$0 = 3x^2+4x-7$$

$$D = 16 +$$

$$6. \sqrt{37-x^2} + 5 = x$$

(6)

$$\sqrt{37-x^2} = x-5 \quad |^2$$

$$37-x^2 = x^2-10x+25$$

$$0 = 2x^2 - 10x - 12$$

$$0 = x^2 - 5x - 6$$

$$0 = (x-6)(x+1)$$

$$\begin{aligned} x_1 &= 6 \\ x_2 &= -1 \end{aligned}$$

$$\text{Sol: } x_1 = 6$$

$$L = \sqrt{37-36} + 5 = 6$$

$$P = 6$$

$$L = P$$

$$x_2 = -1$$

$$L = \sqrt{37-1} + 5 = 6 + 5 = 11$$

$$P = -1$$

$$L \neq P$$

$$7. \sqrt{2x^2+6x+1} = x+2 \quad |^2$$

(1)

$$2x^2+6x+1 = x^2+4x+4$$

$$x^2+2x-3 = 0$$

$$(x+3)(x-1) = 0$$

$$x_1 = -3$$

$$x_2 = 1$$

$$\text{Sol: } x_1 = -3$$

$$L = \sqrt{2 \cdot 9 - 18 + 1} = 1$$

$$P = -3 + 2 = -1$$

$$L \neq P$$

$$x_2 = 1$$

$$L = \sqrt{2+6+1} = 3$$

$$P = 1+2 = 3$$

$$L = P$$

$$8. \sqrt{2x+5} + \sqrt{x+2} = 1$$

(-2)

$$\sqrt{2x+5} = 1 - \sqrt{x+2} \quad |^2$$

$$2x+5 = 1 - 2\sqrt{x+2} + x+2$$

$$x+2 = -2\sqrt{x+2} \quad |^2$$

$$x^2+4x+4 = 4(x+2)$$

$$x^2+4x+4 = 4x+8$$

$$x^2 - 4 = 0$$

$$(x+2)(x-2) = 0$$

$$x_1 = 2 \quad x_2 = -2$$

Sol:

$$x_1 = 2$$

$$L = \sqrt{4+5} + \sqrt{4} = 3 + 2 = 5$$

$$P = 1$$

$$L \neq P$$

$$x_2 = -2$$

$$L = \sqrt{-4+5} + \sqrt{-2+2} = 1$$

$$P = 1$$

$$L = P$$

